

Signal Groups of Clique Compatible Graph in Traffic Control Problems

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Abstract

Signal Groups of clique a compatibility graph is used to solve conflict between the traffic streams and hence can be used as a solution for traffic control problem at an intersection. In this paper we have considered cliques of the compatible graph as signal groups and the set of signal groups which can simultaneously move at an intersection is taken in a phase. Phasing of traffic lights is done by splitting the cycle time among these phases so that each set of signal group is allowed to move once in the cycle.

Keywords : Compatibility Graph, Clique, Conflicting Streams, Phasing and Sequencing, Signal Group, Traffic Control.

1. Introduction

Traffic Theory is a physical phenomenon that aims at understanding and improving automobile traffic, and the problem associated with it such as traffic congestion (Gazis,1970). The traffic control problem is to minimize the waiting time of the public transportation while maintaining the individual traffic flow optimally (Gazis, 2002). A significant development of traffic control systems using traffic lights has been achieved since the first traffic controller was installed in London in 1868. The first green wave was realised in Salt Lake City (U.K.) in 1918, and the first area traffic controller was introduced in Toronto in 1960. At the beginning, electromechanical devices were used to perform traffic control. Then semi conductor-based controllers known as sensors were placed in different places to collect traffic information are used in traffic control system (Gu,W. and Jia X., 2005; 2006). Nowadays, microprocessor based controller are used in Traffic Control Systems. In 1960's a method of combinatorial optimisation approach of Branch and Bound type (Mitten, 1970; Suyudi et al., 2016; 2017; 2018) was used for solving optimal traffic control problems (Locatelli, 2000). The combinatorial approach to the optimal traffic control problem was founded by introducing the *Compatibility* graph of traffic streams (Stoffers, 1968). The most common means of traffic control in modern cities is traffic control by traffic signals. Traffic signals made it possible to solve conflicts between traffic flows at intersections (Guberinic, 2008). This goal however can be achieved in different ways and applications of particular methods have different consequences regarding the intersection capacity, delay, or environmental pollution. Traffic signals are introduced at an intersection to solve conflict between traffic streams in traffic control problems. For solving the control problem it is necessary to know relations between traffic streams at an intersection. By traffic streams we mean the following :

Traffic streams t_i on an intersection are elements of the set of traffic stream, p i.e

$$p = \{ t_1, t_2, \dots, t_i, \dots, t_I \}$$

where $i \in T$ and T is the set of traffic stream indices :

$$T = \{ 1, 2, 3, \dots, i, \dots, I \}$$

Since the main objective of traffic control by traffic lights is to give the right-of-way to some of traffic streams, and to stop others, it is necessary to find, in the set of traffic streams of an intersection, the traffic streams that can simultaneously get the right-of-way. Therefore, a traffic stream compatibility relation is introduced, defined by a set of traffic stream pairs, such that elements of the pair can simultaneously get the right-of-way (Hosseini, 1978; Kadiyali, 2011).

The traffic streams compatibility relation plays an important role in solving traffic control problems related to :

- Deciding whether traffic control by traffic lights should be introduced at an intersection.
- Assigning control variables to traffic streams or to subsets of traffic streams.
- The traffic control process on an intersection.

The factors that have to be considered when defining the compatibility relation are :

- The intersection geometry
- Factors related to traffic process safety, for which expert estimations of traffic engineers are needed.

The analysis of intersection geometry considers mutual relations of traffic streams. When trajectories of two traffic streams do not cross, these streams can simultaneously get the right-of-way i.e. they are compatible. On the other hand, when trajectories of two traffic streams do cross, the streams are in a conflict, and their simultaneous movement through the intersection cannot be permitted. If volumes are not high, a “filtering” of one stream through another can be permitted in some cases. However, when determining the compatibility relation, some special requirements should be taken into account, e.g., some streams are required to pass through the intersection without any disturbance, although filtering could be permitted if only their volumes were considered. These requirements are usually achieved by directional signals (Kadiyali, 2011).

2. Conflicting Relation of Traffic Streams

Some pair of traffic streams use, along a part of their trajectories, the same space on the intersection i.e. the conflict area. These are the streams whose trajectories cross or merge. A conflict exists between such streams. The set of all pairs of traffic streams that creates a conflict between elements of the pairs represents the conflictness relation. Thus the conflictness relation C_1 can be defined as (Kadiyali, 2011):

$$C_1 = \{(t_i, t_j) \mid \text{the trajectories of } t_i \text{ and } t_j \text{ cross or merge, } t_i, t_j \in p\}$$

The graph of conflictness, G_k is defined by set p and the relation C_1 :

$$G_k = (p, C_1)$$

3. Compatibility Relation of Traffic Streams

In determining the compatibility relation of traffic streams, it is necessary to consider the following factors:

- The pairs of conflicting traffic streams that can simultaneously get the right-of-way.
- The traffic streams required to pass through the intersection without any disturbance (the streams to which the right of way is given by directional signals)

Some pairs of conflicting traffic streams can at the same time are pairs of compatible streams, although the streams are conflicting. Therefore, it is necessary to divide the conflicts into allowed or forbidden. Forbidden conflicts can be regulated only by traffic lights, while allowed conflicts are solved by traffic participants themselves, respecting priority rules prescribed by traffic regulations. Without traffic lights, conflicts are solved by “filtering” one stream through another. The possibility of filtering depends on vehicle spacing interval, which depends on volume of traffic streams. The volumes changes during the day. There are intervals with very high volume like morning peak, afternoon peak, and intervals with significantly lower volume like off-peak and night periods. Hence, situations may arise that two conflicting traffic streams may simultaneously have the right-of-way in one period and not in another. Thus, it might be necessary to change the compatibility relation during a day. The compatibility relation is defined as (Hosseini, 1978; Kadiyali, 2011):

$$C_2 = \overline{C_1} = (p \times p) \setminus C_1$$

and the graph of the compatibility, G'_k is defined by the set p and the relation C_2 as

$$G'_k = (p, C_2)$$

4. Traffic Signals

The use of traffic signals for control of conflicting streams of vehicular and pedestrian traffic is extensive in most of the urban areas. As mentioned earlier the first traffic signal is reported to have been used in London in 1868. The traffic signs and signals occupy a significant place in traffic control problem at an intersection Kadiyali (2011).

Traffic signals perform a number of functions :

- They can provide for an orderly movement of traffic.
- When proper geometric layouts and control measures are employed, they can increase the traffic – handling capacity of the intersection.
- They can reduce the frequency of number of accidents.
- Under favourable conditions, they can be coordinated to provide for continuous or nearly continuous movement of traffic at a definite speed along a given route.
- If properly designed and set, they can assign right-of-way impartially to traffic, unlike manual controls which can stop and interrupt traffic streams at personal whim of the traffic controller.

5. Signal Group

Introduction of a traffic control system on an intersection consists of installation of signals that will control traffic streams by different light indications Guberinic (2008). The basic intention of traffic signals is to prevent the simultaneous movement of incompatible traffic streams. Traffic control at an intersection consists of giving and canceling the right-of-way to particular traffic streams. Giving and cancelling the right-of-way is performed by different signal indications. Meaning of indications is assigned by a convention. A green indication for vehicles means allowed passage, while red means forbidden passage. An amber indication, appearing after a green indication, as well as a red-yellow after a red indication, informs the driver that the right-of-way will be changed. The duration of yellow and red-yellow intervals in some countries is determined by traffic regulations, and it is most frequently specified as 3s for amber and 2s for red-amber indication.

Signals that control pedestrian streams usually have only two indications : red (“stop”) and green (“walk”).

The most frequently used sequence of signal indications for vehicles and for pedestrians is as shown in the Figure1 below :

Signal sequence for vehicles



Signal sequence for pedestrians



Legend :

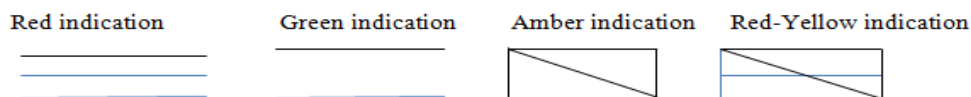


Figure 1. signal indications for vehicles and for pedestrians

The control of traffic lights, i.e. forming and implementing specified signal sequences, is performed by an electronic device called a traffic controller. A controller changes signal indications using sequence of pulses. Changes of signal indications are described by a mathematical variable called a control variable. Control variables can be assigned to every traffic stream. However, the fact that compatible traffic streams can simultaneously gain or lose the right-of-way makes it possible that a subset of traffic streams, comprising several compatible streams can be controlled by a signal control variable. Therefore, it is necessary to establish the correspondence between traffic streams and traffic signals sequences i.e. the control variables that control these traffic streams while introducing traffic lights control at an intersection. The simplest assignment of control variables to traffic streams is to assign one control variable to each traffic stream which is generally not applicable. Various intersection performance indices depend on the choice of traffic control systems for an intersection. Among these performance indices are : total delay or total number of vehicle stops in a defined interval, total flow through the intersection (for saturated intersections). Values of these performance indices also depend on the assignment of control variables to the traffic streams. The best results are, obviously obtained if each traffic stream is controlled by one control variable. When the number of control variables is less than the number of streams, certain constraints have to be introduced that will express the requirement that several traffic streams simultaneously get or lose the right-of-way. The reduction in the number of control variables results in simplification of traffic control problems and also the possibility to use cheaper and simpler traffic controllers Mohsen Hosseini (2009).

Determination of the set of control variables, is in fact, is the problem of partitioning the set of traffic streams, p , in subsets of traffic streams, such that a single control variable can be used to control a subset.

Definition 1 (Kadiyali, 2011). A subset of traffic streams that simultaneously gains or loses the right-of-way i.e. that is controlled by a single controlled variable is called a signal group.

Alternatively, a signal group is defined as the set of traffic streams that are controlled by identical traffic signal indications. For traffic equipment manufacturers, a signal group is a controller module, which always produces one sequence of traffic signal indications.

Definition 2 (Suyudi et al., 2017). A circular arc graph is the intersection graph of a family of arcs on a circle. We say that these arcs are a circular arc representation of the graph.

Definition 3 (Suyudi et al., 2018). A clique of graph G is a complete subgraph of G .

Definition 4 (Suyudi et al., 2018). A clique of graph G is a maximal clique of G if it is not properly contained in another clique of G .

6. An Example

Let us consider a traffic intersection with ten traffic streams as shown in the Figure 2 below:

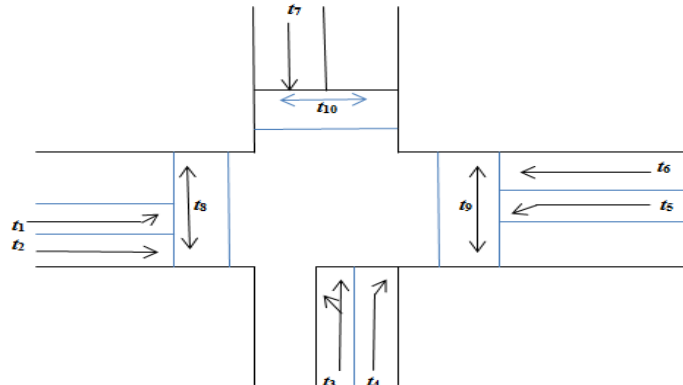


Figure 2: An intersection with ten traffic streams

The above traffic intersection can be represented as a compatibility graph as shown in Figure 3. The graph of this intersection is the compatibility graph, where the nodes represent the traffic streams and if two streams are compatible then it is joined by an edge.

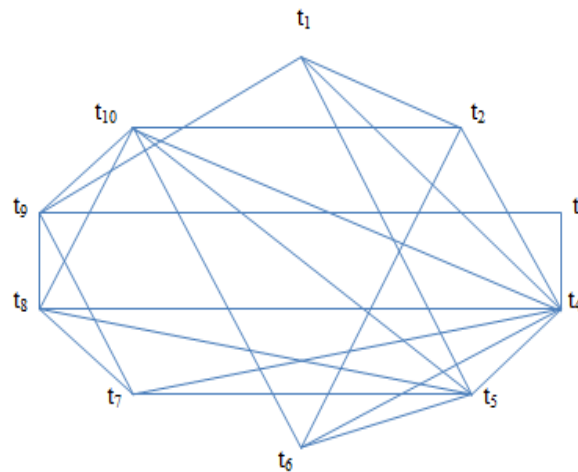


Figure 3. Compatibility Graph of the intersection (Figure 2)

The cliques of a compatible graph are the maximum complete subgraphs of the compatible graph. The set of all the cliques of Figure 3 are:

$$\begin{aligned} & \{t_1, t_2, t_4\}, \{t_1, t_4, t_5\}, \{t_2, t_4, t_6\}, \{t_2, t_4, t_{10}\}, \{t_2, t_6, t_{10}\}, \{t_4, t_5, t_6\}, \\ & \{t_4, t_5, t_7\}, \{t_4, t_5, t_8\}, \{t_4, t_5, t_{10}\}, \{t_4, t_6, t_{10}\}, \{t_4, t_7, t_8\}, \{t_4, t_8, t_{10}\}, \\ & \{t_4, t_5, t_7, t_8\}, \{t_5, t_6, t_{10}\}, \{t_5, t_7, t_8\}, \{t_5, t_8, t_{10}\}, \{t_7, t_8, t_9\}, \{t_8, t_9, t_{10}\} \end{aligned}$$

The cliques can be divided into four signal groups S_1, S_2, S_3 , and S_4 as

$$\begin{aligned} S_1 &= \{\{t_1, t_2, t_4\}, \{t_2, t_4, t_6\}, \{t_2, t_4, t_{10}\}, \{t_2, t_6, t_{10}\}, \{t_8, t_9, t_{10}\}\} \\ S_2 &= \{\{t_1, t_4, t_5\}, \{t_4, t_5, t_7\}, \{t_4, t_7, t_8\}, \{t_4, t_5, t_7, t_8\}, \{t_5, t_7, t_8\}, \{t_7, t_8, t_9\}\} \\ S_3 &= \{\{t_4, t_5, t_6\}, \{t_4, t_5, t_8\}, \{t_4, t_5, t_{10}\}, \{t_4, t_6, t_{10}\}, \{t_4, t_8, t_{10}\}, \{t_5, t_6, t_{10}\}, \{t_5, t_8, t_{10}\}\} \\ S_4 &= \{\{t_3\}\} \end{aligned}$$

This selection of set of signal groups may vary according to the choice of signal groups allowing more number of traffic streams together in their right-of-way. The cliques in S_1 the set can be controlled by a single signal indication i.e. the signal group S_1 will be controlled by one traffic light or by identical signal indications. Similarly, the signal group S_2, S_3 and S_4 can be controlled by identical signal indications.

The cliques in the set S_1 can simultaneously move in the intersection at a time. As the number of streams is more compared to the number of traffic lights certain constraints have to be introduced that will express the requirement that several traffic streams simultaneously get the right-of-way. Although some of streams may conflict while passing through the intersection, however it may be allowed by filtering of traffic streams or by the traffic participants themselves by respecting the priority rules. Similarly the cliques of the signal groups S_2, S_3 and S_4 can simultaneously get the right-of-way in the intersection.

To phase the traffic streams in this intersection, each of the signal group S_1, S_2 and S_3 can be allowed to move once in the cycle. As the traffic stream t_3 conflict with most of the traffic streams, it has to be allowed to move alone in the intersection i.e. all other streams will be stationary when the traffic stream t_3 moves.

As the basic intention of traffic signals at an intersection is to prevent the simultaneous movement of conflicting streams, the vehicle traffic streams will be controlled by four signal indications i.e. red, green, amber and red amber. The signal groups S_1, S_2, S_3 and S_4 can also be controlled by using these signal indications.

Again, if the left turn of the traffic stream t_3 is allowed as conditional compatibility considering the traffic streams which conflict with the traffic stream t_3 exactly once, then it becomes compatible with most of the traffic streams t_1, t_2, t_7 and t_8 etc. The seven additional cliques formed thus increases the number of cliques of the compatibility graph. The additional cliques are

$$\{t_1, t_2, t_3\}, \{t_1, t_3, t_4\}, \{t_2, t_3, t_4\}, \{t_3, t_4, t_7\}, \{t_3, t_4, t_8\}, \{t_3, t_7, t_9\}, \text{ and } \{t_3, t_8, t_9\}$$

as shown in the Figure 4:

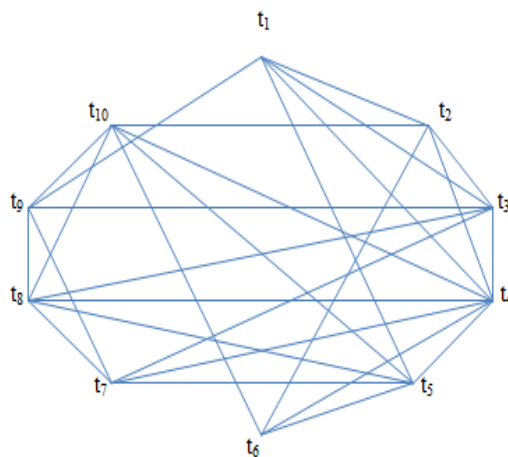


Figure 4: Compatibility Graph of the intersection (Figure 2) when left turn of traffic stream t_3 is allowed

The set of cliques can be divided into the signal groups S_1, S_2, S_3 and S_4 as:

$$\begin{aligned} S_1 &= \{\{t_1, t_2, t_4\}, \{t_2, t_4, t_6\}, \{t_2, t_4, t_{10}\}, \{t_2, t_6, t_{10}\}, \{t_8, t_9, t_{10}\}\} \\ S_2 &= \{\{t_1, t_4, t_5\}, \{t_4, t_5, t_7\}, \{t_4, t_7, t_8\}, \{t_4, t_5, t_7, t_8\}, \{t_5, t_7, t_8\}, \{t_7, t_8, t_9\}\} \\ S_3 &= \{\{t_4, t_5, t_6\}, \{t_4, t_5, t_8\}, \{t_4, t_5, t_{10}\}, \{t_4, t_6, t_{10}\}, \{t_4, t_8, t_{10}\}, \{t_5, t_6, t_{10}\}, \{t_5, t_8, t_{10}\}\} \\ S_4 &= \{\{t_1, t_2, t_3\}, \{t_1, t_3, t_4\}, \{t_2, t_3, t_4\}, \{t_3, t_4, t_7\}, \{t_3, t_4, t_8\}, \{t_3, t_7, t_9\}, \{t_3, t_8, t_9\}\} \end{aligned}$$

Each of these signal groups can be allowed to move once in the cycle. This division of signal group is a better solution as compared to the earlier one as most of the traffic streams are allowed to move at a time i.e. the traffic stream which was conflicting with almost all other streams, now becomes compatible as a result those conflicting traffic streams t_3 are not stationary. In the earlier case when t_3 moves, all other traffic streams are not allowed to move through the intersection, which results in delay; increasing number of vehicles stop; total waiting time etc, this is because the stream t_3 is in conflict with almost all other traffic streams and cannot be allowed to move simultaneously through the intersection.

Again the division of cycle time of the signal groups will be the same as the earlier case i.e. they can be allowed to move once in the cycle and can be controlled by the same signal indications red, green, amber, red-amber. In the compatibility graph of the traffic intersection we shall not consider self loop as a traffic stream is always compatible with itself and not conflict with itself, a loop exist at each of the nodes of the compatible graph which we shall not consider here as the graph is pseudo compatible. In determining the cliques of the compatible graph we shall consider only those cliques which are complete subgraph of the compatibility graph. In graph theory clique in an undirected graph is a subgraph of its vertices such that every two vertices in the

subset is connected by an edge. Here in our problem we shall not consider the cliques which are of one vertex or two vertices as it has no contribution towards any practical solution in a traffic control problem.

The combinatorial approach to the optimal traffic control problem on isolated intersection was founded by Stoffers K. by introducing compatibility graph of the traffic streams. Stoffers also noted that the traffic stream sets with maximum number of non conflicting traffic streams, which can simultaneously get the right-of-way can be determined by extracting cliques of the compatibility graph.

The traffic control on a signalized intersection is performed by means of traffic lights of different colours (green, amber, red and red-amber) that are repeating periodically Mohsen Hosseini (1978). Conflicts between traffic participants are prevented by dividing the cycle time in intervals allocated to traffic flows so that the conflicting flows do not get the right-of-way in the same interval. The control in one interval is defined by one control vector called phase whose components are control variables that control traffic by means of traffic lights. A traffic control problem not only includes the problem of splitting the cycle time into particular phases but also the composition and sequences of the phases. In case of filtering i.e. when filtering is permitted, there exists an interval when two conflicting and compatible vehicle traffic stream get the right-of-way.

7. Phasing and Sequencing of traffic lights at an intersection

The cycle time or cycle length is the time required for one complete sequence of signal indications. Phase is defined as the sequence of conditions applied to one or more streams of traffic which during the cycle receive simultaneous identical signal indication.

To phase traffic light at an intersection of a traffic control problem is to split the cycle time in equal intervals such that every signal group get the right-of-way or allowed to move once in the cycle i.e. all the signal groups can be allowed to move through the intersection most of the time. Here in the problem, in both the cases there are four signal group. If we consider the cycle time to be 60 seconds, each of the signal groups S_1, S_2, S_3 and S_4 can be allowed to move for 15 seconds in the cycle as shown in Figure 5.

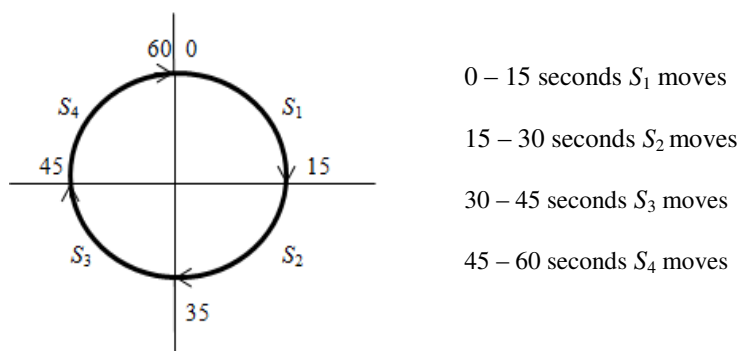


Figure 5: Cycle time of the Signal Groups

In the first case, when the signal groups S_1, S_2 and S_3 move most of the traffic streams get the right-of-way but when the signal group S_4 moves, all the traffic streams are stationary except t_5 as the signal group S_4 conflict with almost all the traffic streams. In the second case, this constrain is overcome as the left turn of the traffic stream t_3 is allowed and hence it become compatible with most of the traffic streams and as a result, these traffic streams is allowed to move when t_3 is allowed. This solution of the division of cycle time is a better one as most of the traffic streams are allowed to move through the intersection at a time i.e. in an interval. This is because the numbers of traffic streams are more compared to the number of traffic lights that control them.

Sequencing of traffic lights, red, green, amber and red-amber at an intersection by giving and cancelling the right-of-way to the signal groups S_1, S_2, S_3 and S_4 can be done by when S_1 get a red indication, S_2 get a red-amber, S_3 moves i.e. a green indication and S_4 an amber indication. The cycle will be repeated and the indication will be changed accordingly, which is shown in the Figure 6 below. This sequencing of traffic lights is same for both the cases.



Figure 35: Sequencing of Signal Indications to Signal Groups

8. Conclusion

Here we have used compatibility graph as a graph theoretic tool to study traffic control problem at an intersection. Traffic signals are used to solve conflict between traffic streams at an intersection and signal groups are used to control traffic streams by different light indications which provides an optimal solution to the control problem. Here we have considered an example of a traffic control problem with two different solutions. In the first case the conflicting streams are not allowed to move simultaneously while in the second case left turn of the conflicting traffic streams are allowed. In terms of accommodating more number of traffic streams in the signal groups, it is found that the solution of the second case is a better one compared to the first case. Finally, it is to be noted that different choice of signal groups e.g. S_1, S_2, S_3 and S_4 of the example will give different solutions of the problem.

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References

- Gazis, D. C. *Traffic Science* (John Wiley & Sons, New York, 1970).
- Gazis, D. C. *Traffic Theory* (Kluwer Academic Publishers, London, 2002).
- Gu, X. W. Jia, On a Traffic Control Problem, *8th International Symposium on Parallel Architectures, Algorithms and Networks* (ISPAN' 05), 2005.
- Gu, X. W. Jia, On a Traffic Sensing Problem, *Preprint, Texas State University*, 2006.
- Guberinic, G. S. and Senborn, B. Lazic, *Optimal Traffic Control Urban Intersection* (CRC Press, 2008).
- Hosseini, F.S.M. *Graph Theory and its Application to the Problems of Society* (SIAM Publications, Philadelphia, 1978).
- Mohsen Hosseini, F.S.M. *Phasing of Traffic Lights at a Road Junction*, *Applied Mathematical Sciences*, Vol. 3, 2009, no. 30, 1487 – 1492.
- Kadiyali, L. R. *Traffic Engineering and Transport Planning* (Khanna Publisher, 2011).
- Locatelli, A. *Optimal Control – An Introduction* (Birkhauser Verlag, 2000).
- Mitten, L.G. Branch and Bound Methods: General Formulation and Properties, *Opns. Res.*, 18, 1970, 24-34.
- Stoffers, E. K. Scheduling of Traffic Lights – A New Approach, *Transportation Research*, 2, 1968, 199.
- Suyudi, M., Mamat, M., & Sukono. An efficient Approach for Traveling Salesman Problem Solution with Branch and Bound. *Proceedings of the International Conference on Industrial Engineering and Operations Management*, 2016, 543-546. Retrieved from www.scopus.com
- Suyudi, M., Mamat, M., Sukono, and Supian, S. Branch and Bound for the Cutwidth Minimization Problem. *Journal of Engineering and Applied Sciences* 12 (Special Issue 1), 5684-5689, 2017. ISSN: 1816-949X.
- Suyudi, M., Sukono, Mamat, and Bon, A.T. Branch and Bound Algorithm for Finding the Maximum Clique Problem. *Proceedings of the International Conference on Industrial Engineering and Operations Management*, Bandung, Indonesia, March 6-8, 2018. Retrieved from www.scopus.com

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